Hands-on Distributional Semantics

Part 2: The parameters of a DSM

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http://wordspace.collocations.de/doku.php/course:esslli2021:start

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Outline

DSM parameters

A taxonomy of DSM parameters Context type & size Feature scaling Measuring distance Dimensionality reduction

Building a DSM

Sparse matrices

Example: a verb-object DSM

Appendix

Taxonomy examples
Three famous DSMs in detail



General definition of DSMs

A distributional semantic model (DSM) is a scaled and/or transformed co-occurrence matrix \mathbf{M} , such that each row \mathbf{x} represents the distribution of a target term across contexts.

	get	see	use	hear	eat	kill
knife	0.027	-0.024	0.206	-0.022	-0.044	-0.042
cat	0.031	0.143	-0.243	-0.015	-0.009	0.131
dog	-0.026	0.021	-0.212	0.064	0.013	0.014
boat	-0.022	0.009	-0.044	-0.040	-0.074	-0.042
cup	-0.014	-0.173	-0.249	-0.099	-0.119	-0.042
pig	-0.069	0.094	-0.158	0.000	0.094	0.265
banana	0.047	-0.139	-0.104	-0.022	0.267	-0.042

Term = word, lemma, phrase, morpheme, word pair, ...

General definition of DSMs

Mathematical notation:

- $k \times n$ co-occurrence matrix $\mathbf{M} \in \mathbb{R}^{k \times n}$ (example: 7×6)
 - ► *k* rows = **target** terms
 - n columns = features or other dimensions

$$\mathbf{M} = \begin{bmatrix} m_{11} & m_{12} & \cdots & m_{1n} \\ m_{21} & m_{22} & \cdots & m_{2n} \\ \vdots & \vdots & & \vdots \\ m_{k1} & m_{k2} & \cdots & m_{kn} \end{bmatrix}$$

- ▶ distribution vector $\mathbf{m}_i = i$ -th row of \mathbf{M} , e.g. $\mathbf{m}_3 = \mathbf{m}_{\mathsf{dog}} \in \mathbb{R}^n$
- ightharpoonup components $\mathbf{m}_i = (m_{i1}, m_{i2}, \dots, m_{in}) = \text{features of } i\text{-th term:}$

$$\mathbf{m}_3 = (-0.026, 0.021, -0.212, 0.064, 0.013, 0.014)$$

= $(m_{31}, m_{32}, m_{33}, m_{34}, m_{35}, m_{36})$



Term-term matrix

Term-term matrix records co-occurrence frequencies with feature terms for each target term

 $\mathbf{m}_{\mathsf{dog}} = \mathsf{collocational}$ profile of $\mathit{dog}\ (pprox \mathsf{word}\ \mathsf{sketch})$

$$\mathbf{M} = \begin{bmatrix} \cdots & \mathbf{m}_1 & \cdots \\ \cdots & \mathbf{m}_2 & \cdots \\ & \vdots & & \\ & \vdots & & \\ \cdots & \mathbf{m}_k & \cdots \end{bmatrix} \qquad \begin{array}{c} \mathsf{an} \\ \mathsf{re} \\ \mathsf{c} \\ \mathsf{e} \end{array}$$

	6.00 d	, <i>!!e</i>	, _V	, hil	ing	140 / S	like _l
cat	83	17	7	37	<u> </u>	1	_
dog	561	13	30	60	1	2	4
nimal	42	10	109	134	13	5	5
time	19	9	29	117	81	34	109
eason	1	_	2	14	68	140	47
cause	_	1	_	4	55	34	55
effect	_	_	1	6	60	35	17

> TT <- DSM TermTerm

> head(TT, Inf) # extract full co-oc matrix from DSM object

Term-context matrix

Term-context matrix records frequency of term in each individual context unit (e.g. document, tweet, encyclopaedia article)

 $\mathbf{f}_{dog} = \text{texts related to or mentioning dogs}$

$$\mathbf{F} = egin{bmatrix} \cdots & \mathbf{f}_1 & \cdots \\ \cdots & \mathbf{f}_2 & \cdots \\ & dots \\ & dots \\ \cdots & \mathbf{f}_k & \cdots \end{bmatrix}$$

	200	<u>ን</u>	_	\ \ \ \			1050 1050 1050 1050		
	Feligh	QÉ	1/6/0	8/034	Phili	Ton Ton	8		
cat	10	10	7	_	<u> </u>	_	_		
dog	_	10	4	11	_	_	_		
animal	2	15	10	2	<u> </u>	_	_		
time	1	_	_	_	2	1	_		
reason	_	1	_	_	1	4	1		
cause	_	-	-	2	1	2	6		
effect		_		1		1			

> TC <- DSM_TermContext

> head(TC, Inf)

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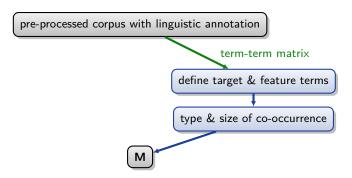
define target & feature terms

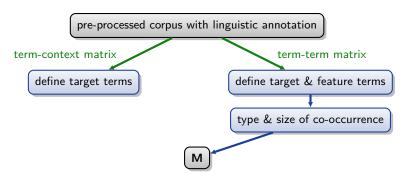
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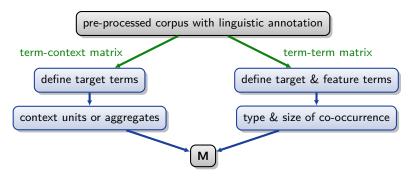
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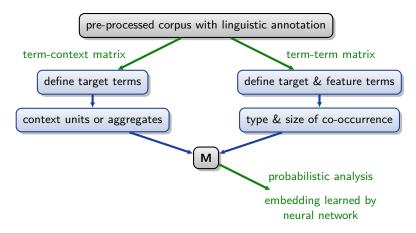
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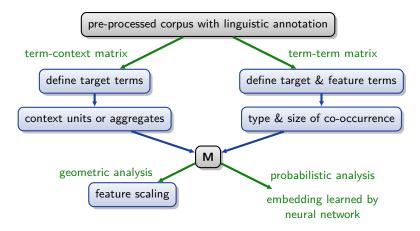
type & size of co-occurrence

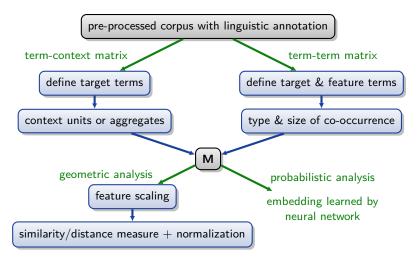


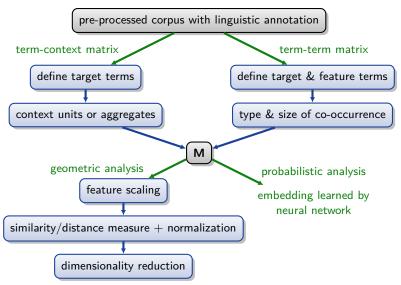


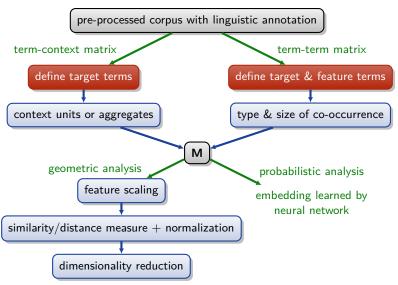












Definition of target and feature terms

- ► Choice of linguistic unit (targets ≠ features)
 - words
 - bigrams, trigrams, . . .
 - multiword units, named entities, phrases, . . .
 - morphemes
 - word pairs (s analogy tasks)

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- Mapping to target/feature terms (→ linguistic annotation)
 - word forms (minimally requires tokenisation)
 - often lemmatisation or stemming to reduce data sparseness: $go, goes, went, gone, going \rightarrow go$
 - ► POS disambiguation (light/N vs. light/A vs. light/V)
 - word sense disambiguation (bank_{river} vs. bank_{finance})
 - ▶ abstraction: POS tags (or *n*-grams of POS tags) as features

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- What is the effect of these choices?



Effects of term mapping

Nearest neighbours of walk (BNC)

word forms

- stroll
- walking
- walked
- ▶ go
- path
- drive
- ▶ ride
- wander
- sprinted
- sauntered

lemmatised + POS

- hurry
- stroll
- stride
- trudge
- amble
- wander
 - walk (noun)
 - walking
- ▶ retrace
- scuttle

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Effects of term mapping

Nearest neighbours of arrivare (Repubblica)

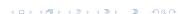
word forms

- giungere
- raggiungere
- arrivi
- raggiungimento
- raggiunto
- trovare
- raggiunge
- arrivasse
- arriverà
- concludere

lemmatised + POS

- giungere
- aspettare
- attendere
- arrivo (noun)
- ricevere
- accontentare
 - approdare
 - pervenire
- venire
 - piombare

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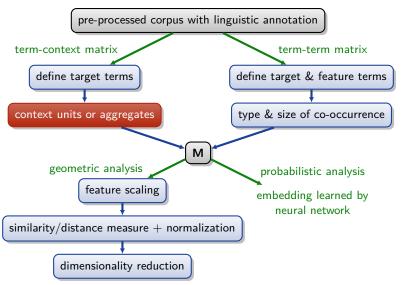
- ► Full-vocabulary models are often unmanageable
 - 762,424 distinct word forms in BNC / 605,910 lemmata
 - ▶ large Web corpora have > 10 million distinct word forms
 - low-frequency targets (and features) are not reliable ("noisy")

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 (high df → uninformative / low df → too sparse to be useful)
 - ▶ alternatives: entropy H or chi-squared statistic X^2

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 (high df → uninformative / low df → too sparse to be useful)
 - ▶ alternatives: entropy H or chi-squared statistic X^2
- Other criteria
 - ▶ POS-based filter: no function words, only verbs, nouns, ...
 - general dictionary, words required for particular task, . . .





Term-context matrix: choice of context unit

- ► Features are usually **tokens** of the selected context unit, i.e. individual instances of a
 - document, novel, Wikipedia article, Web page, . . .
 - paragraph, sentence, tweet, . . .
 - ightharpoonup "co-occurrence" $f_{ij} = \text{frequency of term } i \text{ in context token } j$

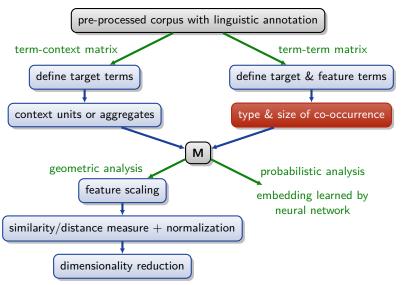
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- Similar context tokens can be aggregated, e.g.
 - feature = cluster of near-duplicate documents
 - feature = syntactic structure of sentence (ignoring content)
 - feature = all tweets from same author ("supertweet")
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- Generalization: context types
 - e.g. pattern of POS tags around target word
 - e.g. subcategorisation pattern of target verb





- Different types of co-occurrence (Evert 2008)
 - surface context (word or character window)
 - textual context (non-overlapping segments)
 - syntactic context (dependency relations)
 - from research into collocations

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 - ▶ unstructured context → acts as a filter for counts
 - ▶ structured context → subcategorizes feature terms
- What effects do you expect from these choices?



Surface context

Context term occurs within a span of k words around target.

The <u>silhouette</u> of the <u>sun</u> beyond a wide-open bay on the lake; the <u>sun</u> still glitters although evening has arrived in Kuhmo. It's midsummer; the living room has its instruments and other objects in each of its corners. [L3/R3 span, k = 6]

- span size (in words or characters)
- symmetric vs. one-sided span
- uniform or "triangular" (distance-based) weighting (don't!)
- spans clamped to sentences or other textual units?

Effect of span size

Nearest neighbours of dog (BNC)

2-word span

- cat
- horse
- ► fox
- pet
- rabbit
- pig
- animal
- mongrel
- sheep
- pigeon

30-word span

- kennel
- puppy
- pet
- bitch
- terrier
- rottweiler
 - canine
- cat
- to bark
- Alsatian

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Textual context

Context term is in the same linguistic unit as target.

The silhouette of the sun beyond a wide-open bay on the lake; the sun still glitters although evening has arrived in Kuhmo. It's midsummer; the living room has its instruments and other objects in each of its corners.

- choice of linguistic unit
 - sentence
 - paragraph
 - ▶ turn in a conversation
 - ▶ Web page
 - tweet
- similar to large surface spans, but more self-contained



Syntactic context

Context term is linked to target by a syntactic dependency (e.g. subject, modifier, . . .).

The silhouette of the sun beyond a wide-open bay on the lake; the sun still glitters although evening has arrived in Kuhmo. It's midsummer; the living room has its instruments and other objects in each of its corners.

- types of syntactic dependency (Padó & Lapata 2007)
- maximal length of dependency path (1 for direct relation)
- homogeneous data (e.g. only verb-object) vs. heterogeneous data (e.g. all children and parents of the verb)

"Knowledge pattern" context

Context term is linked to target by a lexico-syntactic pattern (text mining, cf. Hearst 1992, Pantel & Pennacchiotti 2008, etc.).

In Provence, Van Gogh painted with bright colors such as red and yellow. These colors produce incredible effects on anybody looking at his paintings.

- inventory of lexical patterns
 - ▶ lots of research to identify semantically interesting patterns (cf. Almuhareb & Poesio 2004, Veale & Hao 2008, etc.)
- fixed vs. flexible patterns
 - patterns are mined from large corpora and automatically generalised (optional elements, POS tags or semantic classes)



	features are	
textual / large span	from same topic domain	

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textual / large span	from same topic domain		
small span	collocations		

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syntactic (single relation)	attributes (focus on aspect)

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textual / large span	from same topic domain
small span	collocations
syntactic (single relation)	attributes (focus on aspect)
knowledge pattern	properties

Structured vs. unstructured context

- In unstructered models, context specification acts as a filter
 - determines whether context token counts as co-occurrence
 - e.g. must be linked by any direct syntactic dependency relation

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- In unstructered models, context specification acts as a filter
 - determines whether context token counts as co-occurrence
 - ▶ e.g. must be linked by any direct syntactic dependency relation
- In structured models, feature terms are subtyped
 - depending on their position in the context
 - e.g. left vs. right context, type of syntactic relation, etc.

Structured vs. unstructured surface context

A dog bites a man. The man's dog bites a dog. A dog bites a man.

unstructured	bite
dog	4
man	3

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A dog bites a man. The man's dog bites a dog. A dog bites a man.

structured	bite-L	bite-R
dog	1	3
man	2	1

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data are less sparse (L/R context aggregated)

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structured	bite-L	bite-F
dog	1	3
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more sensitive to semantic distinctions



Structured vs. unstructured dependency context

A dog bites a man. The man's dog bites a dog. A dog bites a man.

data are less sparse (all syntactic relations aggregated)

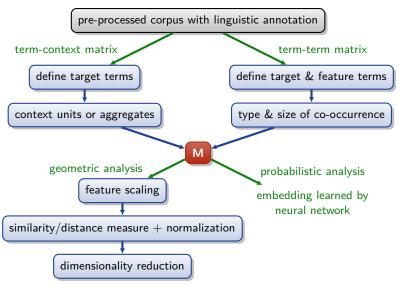
A dog bites a man. The man's dog bites a dog. A dog bites a man.

structured	bite-subj	bite-obj	
dog	3	1	
man	0	2	

more sensitive to semantic distinctions



Building a distributional model



Marginal and expected frequencies

► Matrix of observed co-occurrence frequencies not sufficient

target	feature	0	
dog	small	855	
dog	domesticated	29	

- Notation
 - ► *O* = observed co-occurrence frequency

Marginal and expected frequencies

► Matrix of observed co-occurrence frequencies not sufficient

target	feature	0	R	С	
dog	small	855	33,338	490,580	
dog	domesticated	29	33,338	918	

Notation

- ► *O* = observed co-occurrence frequency
- ightharpoonup R = overall frequency of target term = row marginal frequency
- ► C = overall frequency of feature = column marginal frequency
- $N = \text{sample size} \approx \text{size of corpus}$

Marginal and expected frequencies

Matrix of observed co-occurrence frequencies not sufficient

targe	t feature	0	R	С	E
dog	small	855	33,338	490,580	134.34
dog	domesticated	29	33,338	918	0.25

- Notation
 - ► *O* = observed co-occurrence frequency
 - ightharpoonup R = overall frequency of target term = row marginal frequency
 - ► C = overall frequency of feature = column marginal frequency
 - ▶ $N = \text{sample size} \approx \text{size of corpus}$
- Expected co-occurrence frequency (cf. Evert 2008)

$$E = \frac{R \cdot C}{N} \longleftrightarrow O$$



- Term-document matrix
 - ightharpoonup R = frequency of target term in corpus
 - ► *C* = size of document (# tokens)
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 - # of dependency instances in which target/feature participates
 - ightharpoonup N =total number of dependency instances
 - ▶ N, R, C can be computed from full co-occurrence matrix M

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- Syntactic co-occurrence
 - # of dependency instances in which target/feature participates
 - N = total number of dependency instances
 - ▶ *N*, *R*, *C* can be computed from full co-occurrence matrix **M**
- Textual co-occurrence
 - ▶ *R*, *C*, *O* are "document" frequencies, i.e. number of context units in which target, feature or combination occurs
 - ► N = total # of context units



- Surface co-occurrence
 - ▶ it is quite tricky to obtain fully consistent counts (Evert 2004)
 - recommended: correct E for span size $k (= \# \text{ tokens in span})^1$

$$E = k \cdot \frac{R \cdot C}{N}$$

with R, C = individual corpus frequencies and N = corpus size

 $^{^{1}}$ NB: shifted PPMI (Levy & Goldberg 2014) corresponds to a post-hoc application of the span size adjustment. It performs worse than PPMI, but paper suggests they already approximate correct E by summing over matrix M.

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with R, C = individual corpus frequencies and N = corpus size

- ▶ can also be implemented by pre-multiplying $R' = k \cdot R$ (all pre-compiled surface DSMs in the course)
- ▶ alternatively, compute marginals and sample size by summing over full co-occurrence matrix ($\rightarrow E$ as above, but inflated N)

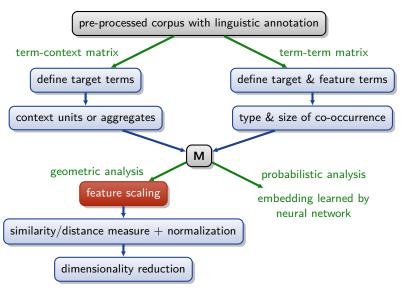
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Marginal frequencies in wordspace

DSM objects in wordspace (class dsm) include marginal frequencies as well as counts of nonzero cells for rows and columns.

```
> TT$rows
   term
              f nnzero
     cat
          22007
    dog 50807
          77053
 animal
   time 1156693
 reason
        95047
        54739
   cause
        133102
 effect
> TT$cols
> TT$globals$N
Γ1] 199902178
> TT$M # the full co-occurrence matrix
```

Building a distributional model



Feature scaling

M is often dominated by few very large entries
 (→ highly skewed frequency distribution due to Zipf's law)

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- M is often dominated by few very large entries
 (→ highly skewed frequency distribution due to Zipf's law)
- Logarithmic scaling: $O' = \log(O + 1)$ (cf. Weber-Fechner law for human perception)
- Statistical association measures (Evert 2004, 2008) take frequency of target term and feature into account
 - usually based on comparison of observed and expected co-occurrence frequency
 - ▶ measures differ in how they balance O and E

Simple association measures

target	feature	0	Ε
dog	small	855	134.34
dog	domesticated	29	0.25
dog	sgjkj	1	0.00027

Simple association measures

pointwise Mutual Information (MI)

$$\mathsf{MI} = \log_2 \frac{O}{E}$$

_	feature	0	Ε	MI	
dog	small	855	134.34	2.67	
dog	domesticated	29	0.25	6.85	
dog	sgiki	1	0.00027	11.85	

DSM parameters

Simple association measures

pointwise Mutual Information (MI)

$$\mathsf{MI} = \log_2 \frac{O}{E}$$

► local MI

$$local-MI = O \cdot MI = O \cdot log_2 \frac{O}{E}$$

targ	get feature	0	Ε	MI	local-MI	
dog	small	855	134.34	2.67	2282.88	
dog	domesticated	29	0.25	6.85	198.76	
dog	· sgjkj	1	0.00027	11.85	11.85	

Simple association measures

pointwise Mutual Information (MI)

$$\mathsf{MI} = \log_2 \frac{O}{E}$$

► local MI

$$local-MI = O \cdot MI = O \cdot log_2 \frac{O}{E}$$

t-score

$$t = \frac{O - E}{\sqrt{O}}$$

 \Box

target	reature	U	L	IVII	local-IVII	t-score
dog	small	855	134.34	2.67	2282.88	24.64
dog	domesticated	29	0.25	6.85	198.76	5.34
dog	sgjkj	1	0.00027	11.85	11.85	1.00

Other association measures

▶ simple log-likelihood (\approx local-MI)

$$G^2 = \pm 2 \cdot \left(O \cdot \log_2 \frac{O}{E} - (O - E) \right)$$

with positive sign for O > E and negative sign for O < E

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$$\mathsf{Dice} = \frac{2O}{R+C}$$

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with positive sign for O > E and negative sign for O < E

Dice coefficient

$$Dice = \frac{2O}{R+C}$$

- ▶ Many other association measures (AMs) available, often based on full contingency tables (see Evert 2008)
 - ▶ http://www.collocations.de/
 - ▶ http://sigil.r-forge.r-project.org/



Applying association scores in wordspace

```
> options(digits=3) # print fractional values with limited precision

> dsm.score(TT, score="MI", sparse=FALSE, matrix=TRUE)

    breed tail feed kill important explain likely

cat 6.21 4.568 3.129 2.801 -Inf 0.0182 -Inf

dog 7.78 3.081 3.922 2.323 -3.774 -1.1888 -0.4958

animal 3.50 2.132 4.747 2.832 -0.674 -0.4677 -0.0966

time -1.65 -2.236 -0.729 -1.097 -1.728 -1.2382 0.6392

reason -2.30 -Inf -1.982 -0.388 1.472 4.0368 2.8860

cause -Inf -0.834 -Inf -2.177 1.900 2.8329 4.0691

effect -Inf -2.116 -2.468 -2.459 0.791 1.6312 0.9221
```

Applying association scores in wordspace

- sparseness of matrix representation is lost (try with TC!)
- cells with score $x = -\infty$ are inconvenient
- distribution of scores may be even more skewed than co-occurrence frequencies themselves (esp. for G^2)

Sparse association measures

► Sparse association scores are cut off at zero, i.e.

$$f(x) = \begin{cases} x & x > 0 \\ 0 & x \le 0 \end{cases}$$

- Also known as "positive" scores
 - ▶ PPMI = positive pointwise MI (e.g. Bullinaria & Levy 2007)
 - ▶ wordspace computes sparse AMs by default → "MI" = PPMI

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 - ightharpoonup sparseness may even increase: cells with x < 0 become empty

Sparse association measures

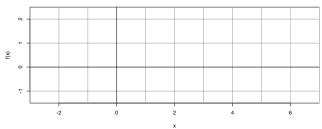
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 - ightharpoonup sparseness may even increase: cells with x < 0 become empty
- ► Further thinning may be beneficial (Polajnar & Clark 2014)
 - ▶ apply shifted cutoff threshold $x > \theta$ (Levy *et al.* 2015)
 - keep only k top-scoring features for each target



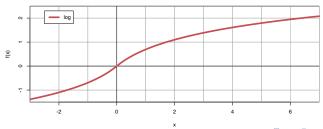
An additional scale transformation can be applied in order to de-skew association scores:



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signed logarithmic transformation

$$f(x) = \pm \log(|x| + 1)$$



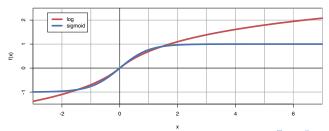
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sigmoid transformation as soft binarization

$$f(x) = \tanh x$$



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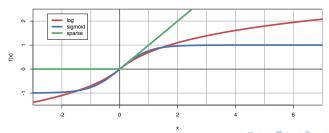
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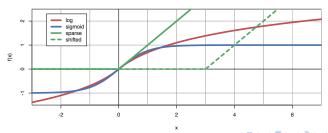
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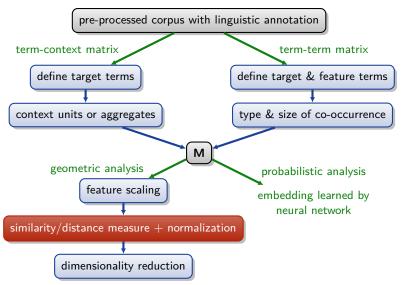
sparse AM as (shifted) cutoff transformation (aka. ReLU)



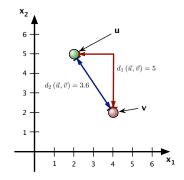
Association scores & transformations in wordspace

```
> dsm.score(TT, score="MI", matrix=TRUE) # PPMI
      breed tail feed kill important explain likely
cat 6.21 4.57 3.13 2.80
                             0.000 0.0182 0.000
dog 7.78 3.08 3.92 2.32 0.000 0.0000 0.000
animal 3.50 2.13 4.75 2.83 0.000 0.0000 0.000
time 0.00 0.00 0.00 0.00 0.000 0.0000 0.639
reason 0.00 0.00 0.00 0.00 1.472 4.0368 2.886
cause 0.00 0.00 0.00 0.00 1.900 2.8329 4.069
effect 0.00 0.00 0.00 0.00 0.791 1.6312 0.922
> dsm.score(TT, score="simple-ll", matrix=TRUE)
> dsm.score(TT, score="simple-ll", transf="log", matrix=T)
# logarithmic co-occurrence frequency
> dsm.score(TT, score="freq", transform="log", matrix=T)
# now try other parameter combinations
> ?dsm.score # read help page for available parameter settings
```

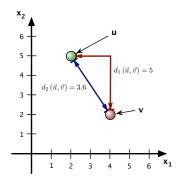
Building a distributional model



- **Distance** between vectors $\mathbf{u}, \mathbf{v} \in \mathbb{R}^n$ → (dis)similarity
 - $\mathbf{u} = (u_1, \dots, u_n)$
 - $\mathbf{v} = (v_1, \ldots, v_n)$

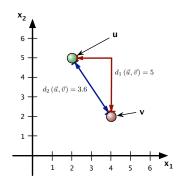


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- **Euclidean** distance $d_2(\mathbf{u}, \mathbf{v})$



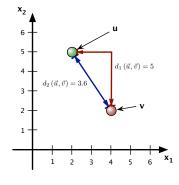
$$d_2(\mathbf{u},\mathbf{v}) := \sqrt{(u_1 - v_1)^2 + \dots + (u_n - v_n)^2}$$

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- "City block" Manhattan distance $d_1(\mathbf{u}, \mathbf{v})$



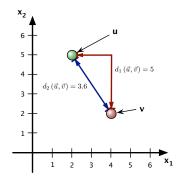
$$d_1(\mathbf{u},\mathbf{v}) := |u_1 - v_1| + \cdots + |u_n - v_n|$$

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- "City block" Manhattan distance d₁ (u, v)
- ▶ Both are special cases of the Minkowski p-distance $d_p(\mathbf{u}, \mathbf{v})$ (for $p \in [1, \infty]$)



$$d_p(\mathbf{u},\mathbf{v}) := (|u_1 - v_1|^p + \cdots + |u_n - v_n|^p)^{1/p}$$

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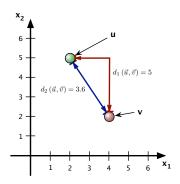


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$$d_{\infty}(\mathbf{u}, \mathbf{v}) = \max\{|u_{1} - v_{1}|, \dots, |u_{n} - v_{n}|\}$$



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 - $\mathbf{u} = (u_1, \ldots, u_n)$
 - $\mathbf{v} = (v_1, \dots, v_n)$
- **Hamming** distance $d_0(\mathbf{u}, \mathbf{v})$ not very useful for DSM
- Extension of the Minkowski p-distance d_p (u, v) (for 0



$$d_p(\mathbf{u}, \mathbf{v}) := |u_1 - v_1|^p + \dots + |u_n - v_n|^p$$
$$d_0(\mathbf{u}, \mathbf{v}) = \#\{i \mid u_i \neq v_i\}$$

Computing distances

```
Preparation: store "scored" matrix in DSM object
```

```
> TT <- dsm.score(TT, score="freq", transform="log")
```

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Compute distances between individual term pairs . . .

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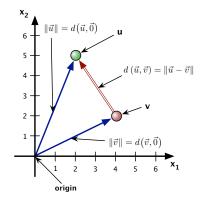
Compute distances between individual term pairs . . .

... or full distance matrix.

```
> dist.matrix(TT, method="euclidean")
> dist.matrix(TT, method="minkowski", p=4)
```

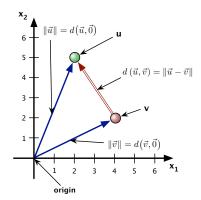
Distance and vector length = norm

- Intuitively, distance $d(\mathbf{u}, \mathbf{v})$ should correspond to length $\|\mathbf{u} \mathbf{v}\|$ of displacement vector $\mathbf{u} \mathbf{v}$
 - $ightharpoonup d(\mathbf{u}, \mathbf{v})$ is a metric
 - ▶ $\|\mathbf{u} \mathbf{v}\|$ is a **norm**
 - $\|\mathbf{u}\| = d(\mathbf{u}, \mathbf{0})$



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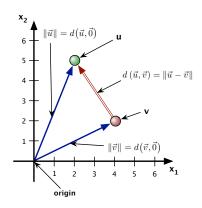
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- Any norm-induced metric is translation-invariant
- Minkowski *p*-norm with $d_p(\mathbf{u}, \mathbf{v}) = \|\mathbf{u} \mathbf{v}\|_p$

$$\|\mathbf{u}\|_{p} := (|u_{1}|^{p} + \dots + |u_{n}|^{p})^{1/p}$$

$$\|\mathbf{u}\|_{p} := |u_{1}|^{p} + \dots + |u_{n}|^{p}$$

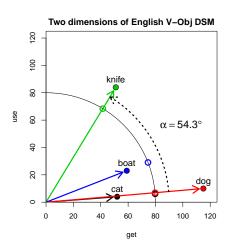
$$\|\mathbf{u}\|_{0} = \#\{i \mid u_{i} \neq 0\}$$



for
$$1 \leq p$$
 for $0 \leq p < 1$ (an F-norm) $\|\mathbf{u}\|_{\infty} = \max\{|u_1|, \dots, |u_n|\}$

Normalisation of row vectors

▶ Part 1: geometric distances only meaningful for vectors of the same length ||x||



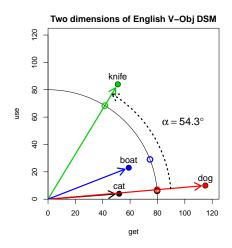
Normalisation of row vectors

- Part 1: geometric distances only meaningful for vectors of the same length ||x||
- Normalize by scalar division:

$$\mathbf{x}' = \frac{1}{\|\mathbf{x}\|} \cdot \mathbf{x} = \left(\frac{x_1}{\|\mathbf{x}\|}, \frac{x_2}{\|\mathbf{x}\|}, \ldots\right)$$

with
$$\|\mathbf{x}'\|=1$$

Norm must be compatible with distance measure!



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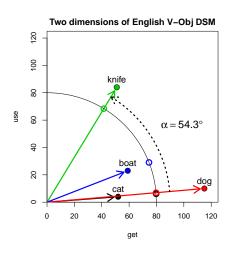
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$$\|\mathbf{x}'\|=1$$

- Norm must be compatible with distance measure!
- Special case: scale x ≥ 0 to stochastic vector with

$$\|\mathbf{x}\|_1 = |x_1| + \cdots + |x_n|$$

→ probabilistic interpretation



Norms and normalization

```
> rowNorms(TT$S, method="euclidean")
cat dog animal time reason cause effect
6.90 8.96 8.82 10.29 8.13 6.86 6.52
```

```
> TT <- dsm.score(TT, score="freq", transform="log",
                  normalize=TRUE, method="euclidean")
> rowNorms(TT$S, method="euclidean") # all = 1 now
> dist.matrix(TT, method="euclidean")
             dog animal time reason cause effect
cat 0.000 0.224 0.473 0.782 1.121 1.239 1.161
dog 0.224 0.000 0.398 0.698 1.065 1.179 1.113
animal 0.473 0.398 0.000 0.426 0.841 0.971 0.860
time 0.782 0.698 0.426 0.000 0.475 0.585 0.502
reason 1.121 1.065 0.841 0.475 0.000 0.277 0.198
cause 1.239 1.179 0.971 0.585 0.277 0.000 0.224
effect 1.161 1.113 0.860 0.502 0.198 0.224 0.000
```

Distance measures for non-negative vectors

▶ Information theory: Kullback-Leibler (KL) divergence for stochastic vectors (non-negative $\mathbf{x} \ge 0$ and $\|\mathbf{x}\|_1 = 1$)

$$D(\mathbf{u}\|\mathbf{v}) = \sum_{i=1}^n u_i \cdot \log_2 \frac{u_i}{v_i}$$

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- Properties of KL divergence
 - most appropriate for a probabilistic interpretation of M
 - ightharpoonup zeroes in $m {f v}$ without corresponding zeroes in $m {f u}$ are problematic
 - ▶ not symmetric, unlike geometric distance measures
 - ▶ alternatives: skew divergence, Jensen-Shannon divergence

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- ► A symmetric distance metric (Endres & Schindelin 2003)

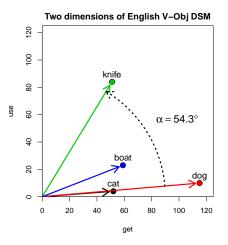
$$D_{\mathbf{u}\mathbf{v}} = D(\mathbf{u}\|\mathbf{z}) + D(\mathbf{v}\|\mathbf{z})$$
 with $\mathbf{z} = \frac{\mathbf{u} + \mathbf{v}}{2}$



Similarity measures

Angle α between vectors $\mathbf{u}, \mathbf{v} \in \mathbb{R}^n$ is given by

$$\cos \alpha = \frac{\sum_{i=1}^{n} u_i \cdot v_i}{\sqrt{\sum_i u_i^2} \cdot \sqrt{\sum_i v_i^2}}$$
$$= \frac{\mathbf{u}^T \mathbf{v}}{\|\mathbf{u}\|_2 \cdot \|\mathbf{v}\|_2}$$

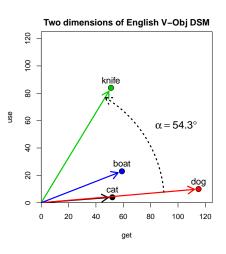


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$$= \frac{\mathbf{u}^T \mathbf{v}}{\|\mathbf{u}\|_2 \cdot \|\mathbf{v}\|_2}$$

- cosine measure of similarity: cos α
 - ▶ $\cos \alpha = 1$ → collinear
 - ► $\cos \alpha = 0$ → orthogonal
- Corresponding metric: angular distance α



Euclidean distance or cosine similarity?

$$d_{2}(\mathbf{u}, \mathbf{v}) = \|\mathbf{u} - \mathbf{v}\|_{2} = \sqrt{\sum_{i} (u_{i} - v_{i})^{2}}$$

$$= \sqrt{\sum_{i} u_{i}^{2} + \sum_{i} v_{i}^{2} - 2\sum_{i} u_{i}v_{i}}$$

$$= \sqrt{\|\mathbf{u}\|_{2}^{2} + \|\mathbf{v}\|_{2}^{2} - 2\mathbf{u}^{T}\mathbf{v}}$$

$$= \sqrt{2 - 2\cos\phi}$$

 $d_2(\mathbf{u},\mathbf{v})$ is a monotonically increasing function of ϕ

Similarity measures for non-negative vectors

Generalized Jaccard coefficient = shared features

$$J(\mathbf{u}, \mathbf{v}) = \frac{\sum_{i=1}^{n} \min\{u_i, v_i\}}{\sum_{i=1}^{n} \max\{u_i, v_i\}}$$

▶ $1 - J(\mathbf{u}, \mathbf{v})$ is a distance **metric** (Kosub 2016)

Similarity measures for non-negative vectors

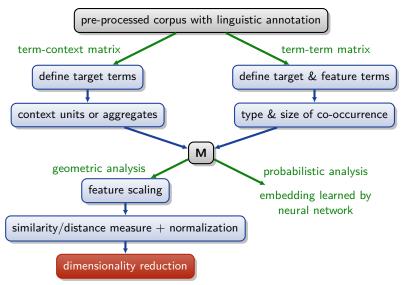
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- ▶ $1 J(\mathbf{u}, \mathbf{v})$ is a distance **metric** (Kosub 2016)
- ► An asymmetric measure of feature overlap (Clarke 2009)

$$o(\mathbf{u},\mathbf{v}) = \frac{\sum_{i=1}^{n} \min\{u_i,v_i\}}{\sum_{i=1}^{n} u_i}$$

Building a distributional model



Dimensionality reduction = model compression

- ➤ Co-occurrence matrix M is often unmanageably large and can be extremely sparse
 - ► Google Web1T5: 1M × 1M matrix with one trillion cells, of which less than 0.05% contain nonzero counts (Evert 2010)
- Compress matrix by reducing dimensionality (= rows)

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 - measured by entropy, chi-squared test, nonzero count, . . .
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 - measured by entropy, chi-squared test, nonzero count, . . .
 - may select similar dimensions and discard valuable information
- Projection into (linear) subspace
 - principal component analysis (PCA)
 - independent component analysis (ICA)
 - random indexing (RI)
 - intuition: preserve distances between data points



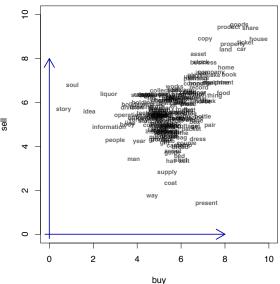
Dimensionality reduction & latent dimensions

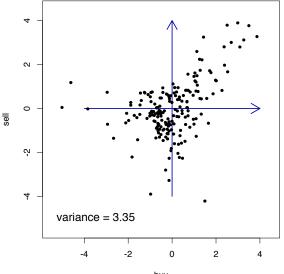
Landauer & Dumais (1997) claim that LSA dimensionality reduction (and related PCA technique) uncovers **latent** dimensions by exploiting correlations between features.

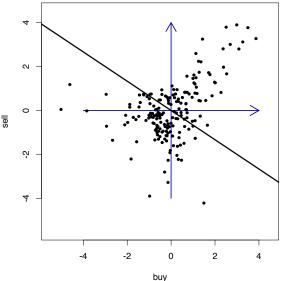
- Example: term-term matrix
- V-Obj co-oc. extracted from BNC
 - ▶ targets = noun lemmas
 - features = verb lemmas
- feature scaling: association scores (SketchEngine log Dice)
- ▶ k = 186 nouns with $f_{\text{buy}} + f_{\text{sell}} \ge 25$
- ightharpoonup n = 2 dimensions: buy and sell

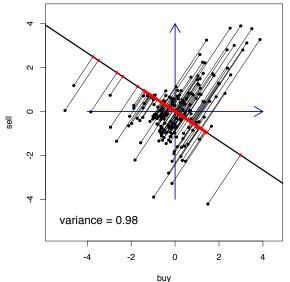
noun	buy	sell
antique	5.12	5.50
bread	5.96	3.99
computer	6.75	6.83
factory	4.95	4.72
group	4.93	4.28
jewellery	5.11	5.73
mill	5.14	5.41
people	3.00	4.26
record	6.81	6.68
souvenir	5.45	4.67
ticket	8.93	8.74

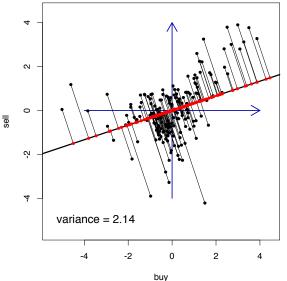
Dimensionality reduction & latent dimensions

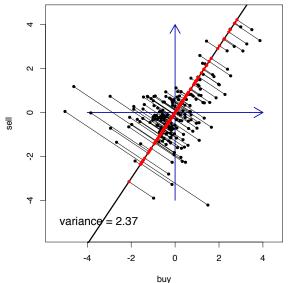


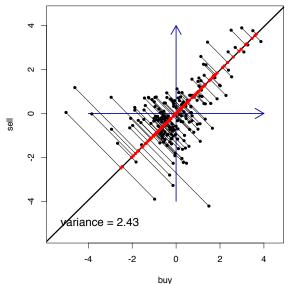




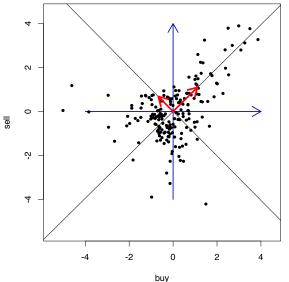




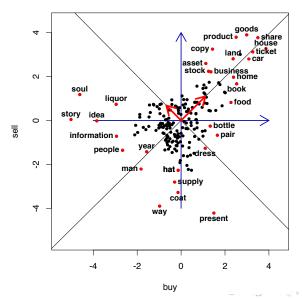




PCA dimensionality reduction: further dimensions



PCA dimensionality reduction: further dimensions



PCA dimensionality reduction

- Principal component analysis (PCA)
 - orthogonal projection into orthogonal latent dimensions
 - finds optimal subspace of given dimensionality (such that orthogonal projection preserves distance information)
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 - the mathematical algorithm behind PCA
 - often applied without centering in distributional semantics
 - optimality of subspace not guaranteed
 - \blacksquare first dimension(s) uninteresting (\mapsto non-negative quadrant)

PCA dimensionality reduction

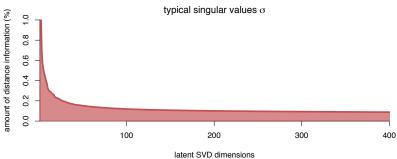
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 - $\quad \text{first dimension(s) uninteresting } (\mapsto \text{non-negative quadrant})$
- NB: row vectors should be renormalised after PCA/SVD
 - unless cosine similarity / angular distance is used
 - also normalise vectors before dimensionality reduction



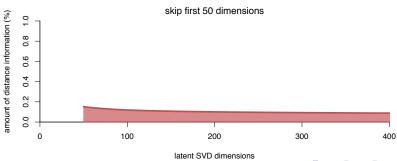
Dimensionality reduction in practice

```
# SVD is the algorithm behind PCA dimensionality reduction
> TT2 <- dsm.projection(TT, n=2, method="svd")
> TT2
        svd1 svd2
cat. -0.733 - 0.6615
dog -0.782 -0.6110
animal -0.914 -0.3606
time -0.993 0.0302
reason -0.889 0.4339
cause -0.817 0.5615
effect -0.871 0.4794
> x <- TT2[, 1] # first latent dimension
> y <- TT2[, 2] # second latent dimension
> plot(x, y, pch=20, col="red",
       xlim=extendrange(x), ylim=extendrange(y))
> text(x, y, rownames(TT2), pos=3)
```

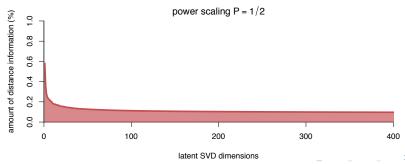
► Truncated SVD omits latent dimensions that capture relatively little distance information (here r = 400)



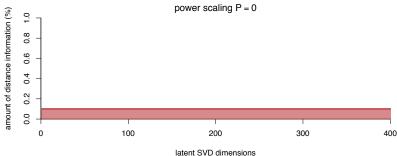
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- ▶ Power-scaling of dimensions: σ^P (Caron 2001)
 - ▶ Bullinaria & Levy (2012) report positive effect



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- ▶ Power-scaling of dimensions: σ^P (Caron 2001)
 - ▶ Bullinaria & Levy (2012) report positive effect
 - esp. with P = 0 to equalize dimensions (whitening)

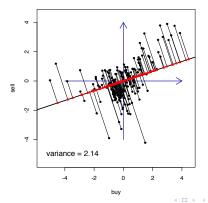


Power-scaling in practice

```
> TT2 <- dsm.projection(TT, n=2, method="svd", power=0)
> TT2
        svd1 svd2
cat. -0.322 - 0.5110
dog -0.343 -0.4721
animal -0.401 -0.2786
time -0.436 0.0233
reason -0.390 0.3353
cause -0.359 0.4338
effect -0.383 0.3704
# power-scaling can also be applied post-hoc
> sigma <- attr(TT2, "sigma")</pre>
                              # singular values
> scaleMargins(TT2, cols=sigma^{0.5}) \# P = 1/2
> scaleMargins(TT2, cols=sigma) # unscaled (P = 1)
```

Dimensionality reduction by RI

- ► Random indexing (RI)
 - ▶ project into random subspace (Sahlgren & Karlgren 2005)
 - reasonably good if there are many subspace dimensions
 - ► can be performed online w/o collecting full co-oc. matrix



Outline

DSM parameters

A taxonomy of DSM parameters
Context type & size

Feature scaling

Measuring distance

Dimensionality reduction

Building a DSM

Sparse matrices

Example: a verb-object DSN

Appendix

Taxonomy examples

Three famous DSMs in detail

Scaling up to the real world

- ► So far, we have worked on minuscule **toy models**
- We want to scale up to real world data sets now

Scaling up to the real world

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- ► Example 1: span-based DSM on BNC content words
 - ▶ 83,926 lemma types with $f \ge 10$
 - ▶ term-term matrix with $83,926 \cdot 83,926 = 7$ billion entries
 - standard representation requires 56 GB of RAM (8-byte floats)
 - ▶ only 22.1 million non-zero entries (= 0.32%)

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 - standard representation requires 56 GB of RAM (8-byte floats)
 - ▶ only 22.1 million non-zero entries (= 0.32%)
- ► Example 2: Google Web 1T 5-grams (1 trillion words)
 - ▶ more than 1 million word types with $f \ge 2500$
 - term-term matrix with 1 trillion entries requires 8 TB RAM
 - only 400 million non-zero entries (= 0.04%)



Sparse matrix representation

► Invented example of a **sparsely populated** DSM matrix

	eat	get	hear	kill	see	use
boat		59			39	23
cat	•	•		26	58	•
cup	•	98				
dog	33	•	42		83	
knife	•	•				84
pig	9			27		

Sparse matrix representation

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knife	•	•	•	•		84
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Store only non-zero entries in compact sparse matrix format

row	col	value	row	col	value
1	2	59	4	1	33
1	5	39	4	3	42
1	6	23	4	5	83
2	4	26	5	6	84
2	5	58	6	1	9
3	2	98	6	4	27

Working with sparse matrices

- Compressed format: each row index (or column index) stored only once, followed by non-zero entries in this row (or column)
 - convention: column-major matrix (data stored by columns)
- Specialised algorithms for sparse matrix algebra
 - especially matrix multiplication, solving linear systems, etc.
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Working with sparse matrices

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- Specialised algorithms for sparse matrix algebra
 - especially matrix multiplication, solving linear systems, etc.
 - take care to avoid operations that create a dense matrix!
- ▶ R implementation: Matrix package
 - essential for real-life distributional semantics
 - wordspace provides additional support for sparse matrices (vector distances, sparse SVD, ...)
- Other software: Matlab, Octave, Python + SciPy
 - TensorFlow, PyTorch, ... always use dense matrices!



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Triplet tables

- ► A sparse DSM matrix can be represented as a table of triplets (target, feature, co-occurrence frequency)
 - for syntactic co-occurrence and term-document matrices, marginals can be computed from a complete triplet table
 - ▶ for surface and textual co-occurrence, marginals have to be provided in separate files (see ?read.dsm.triplet)

noun	rel	verb	f	mode
dog	subj	bite	3	spoken
dog	subj	bite	12	written
dog	obj	bite	4	written
dog	obj	stroke	3	written

- ▶ DSM_VerbNounTriples_BNC contains additional information
 - syntactic relation between noun and verb
 - written or spoken part of the British National Corpus



Constructing a DSM from a triplet table

 Additional information can be used for filtering (verb-object relation), or aggregate frequencies (spoken + written BNC)

```
> tri <- subset(DSM_VerbNounTriples_BNC, rel == "obj")
```

- Construct DSM object from triplet input
 - raw.freq=TRUE indicates raw co-occurrence frequencies (rather than a pre-weighted DSM)
 - constructor aggregates counts from duplicate entries
 - marginal frequencies are automatically computed

> VObj # inspect marginal frequencies (e.g. head(VObj\$rows, 20))

Exploring the DSM

```
> VObj <- dsm.score(VObj, score="MI", normalize=TRUE)</pre>
> nearest.neighbours(VObj, "dog") # angular distance
                 animal rabbit fish
  horse
          cat
                                          guy
   73.9 75.9 76.2 77.0 77.2 78.5
cichlid kid bee creature
   78.6 79.0 79.1 79.5
> nearest.neighbours(VObj, "dog", method="manhattan")
# NB: we used an incompatible Euclidean normalization!
> VObj50 <- dsm.projection(VObj, n=50, method="svd")
> nearest.neighbours(VObj50, "dog")
```

Practice

- Code examples and further explanations: hands_on_day2.R
- How many different models can you build from DSM_VerbNounTriples_BNC?
 - apply different filters, scores, transformations and metrics
 - explore nearest neighbours of selected word
- Build real-life DSMs from pre-compiled co-occurrence data
 - http://wordspace.collocations.de/doku.php/course:material
 - load pre-compiled matrix and apply different parameters
 - compare nearest neighbours or semantic maps
- ► Learn how to import your own co-occurrence data

 Rearn how to import your own co-occurrence data

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 - download example data sets to subdirectory data/



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Latent Semantic Analysis (Landauer & Dumais 1997)

- term-context matrix with document context
- weighting: log term frequency and term entropy
- distance measure: cosine
- dimensionality reduction: SVD

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Hyperspace Analogue to Language (Lund & Burgess 1996)

- term-term matrix with surface context
- structured (left/right) and distance-weighted frequency counts
- ▶ distance measure: Minkowski metric $(1 \le p \le 2)$
- dimensionality reduction: feature selection (high variance)



Infomap NLP (Widdows 2004)

- term-term matrix with unstructured surface context
- weighting: none
- distance measure: cosine
- dimensionality reduction: SVD

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- weighting: none
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Random Indexing (Karlgren & Sahlgren 2001)

- term-term matrix with unstructured surface context
- weighting: various methods
- distance measure: various methods
- dimensionality reduction: random indexing (RI)



Dependency Vectors (Padó & Lapata 2007)

- term-term matrix with unstructured dependency context
- weighting: log-likelihood ratio
- distance measure: PPMI-weighted Dice (Lin 1998)
- dimensionality reduction: none

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Distributional Memory (Baroni & Lenci 2010)

- term-term matrix with structured and unstructered dependencies + knowledge patterns
- weighting: local-MI on type frequencies of link patterns
- distance measure: cosine
- dimensionality reduction: none



... and an unexpected application

Authorship attribution (Burrows 2002)

- Burrows's Delta method is very popular in modern literary stylometry and authorship attribution (Evert et al. 2017)
- document-term matrix with word forms as features
- weighting: relative frequency of word form in document
- ▶ feature selection: 200–5,000 most frequent words (mfw)
- ► columns are standardized ($\mu = 0$, $\sigma^2 = 1$) → z-scores
- clustering of documents based on various distance metrics (or nearest-neighbour classifier for known authors)
- dimensionality reduction: none
- ▶ main result: angle/cosine > Manhattan > Euclidean



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Latent Semantic Analysis (Landauer & Dumais 1997)

- ► Corpus: 30,473 articles from Grolier's *Academic American Encyclopedia* (4.6 million words in total)
 - articles were limited to first 2,000 characters
- Word-article frequency matrix for 60,768 words
 - row vector shows frequency of word in each article
- Logarithmic frequencies scaled by word entropy
- Reduced to 300 dim. by singular value decomposition (SVD)
 - borrowed from LSI (Dumais et al. 1988)
 - central claim: SVD reveals latent semantic features, not just a data reduction technique
- Evaluated on TOEFL synonym test (80 items)
 - ▶ LSA model achieved 64.4% correct answers
 - ▶ also simulation of learning rate based on TOEFL results

Word Space (Schütze 1992, 1993, 1998)

- ightharpoonup Corpus: pprox 60 million words of news messages
 - from the New York Times News Service
- Word-word co-occurrence matrix
 - ▶ 20,000 target words & 2,000 context words as features
 - row vector records how often each context word occurs close to the target word (co-occurrence)
 - ▶ co-occurrence window: left/right 50 words (Schütze 1998) or \approx 1000 characters (Schütze 1992)
- Rows weighted by inverse document frequency (tf.idf)
- Context vector = centroid of word vectors (bag-of-words)
 - goal: determine "meaning" of a context
- Reduced to 100 SVD dimensions (mainly for efficiency)
- Evaluated on unsupervised word sense induction by clustering of context vectors (for an ambiguous word)
 - induced word senses improve information retrieval performance



HAL (Lund & Burgess 1996)

- ► HAL = Hyperspace Analogue to Language
- Corpus: 160 million words from newsgroup postings
- ► Word-word co-occurrence matrix
 - same 70,000 words used as targets and features
 - ► co-occurrence window of 1 10 words
- Separate counts for left and right co-occurrence
 - i.e. the context is structured
- ► In later work, co-occurrences are weighted by (inverse) distance (Li *et al.* 2000)
 - but no dimensionality reduction
- Applications include construction of semantic vocabulary maps by multidimensional scaling to 2 dimensions



HAL (Lund & Burgess 1996)

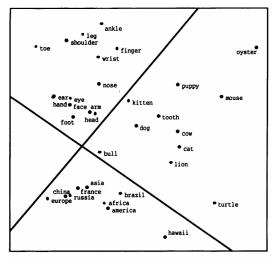


Figure 2. Multidimensional scaling of co-occurrence vectors.



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